

Symbol	Meaning	Type of Object
\vec{E}	Electric Field	Vector field
\vec{B}	Magnetic Field	Vector field
ϵ_0	permittivity constant	constant
μ_0	Permeability constant	constant
c	speed of light	constant
k	Coulomb's constant: $\frac{1}{4\pi\epsilon_0}$	constant
σ	Closed orientable surface	
C	Curve	simple closed piecewise smooth curve
\vec{n}	Outward unit normal vector, normal to the surface σ	vector-valued function
\vec{T}	Unit tangent vector, tangent to the curve C	vector-valued function
q_{enc}	Charge enclosed by the surface	
ρ	charge density	charge per unit volume
\vec{J}	current density vector	vector-valued function: magnitude = current per unit area, direction = same or opposite the velocity of the moving charges, depending on their sign
i_{enc}	current encircled by the closed curve C	
Φ_E	electric flux	
Φ_B	magnetic flux	
$\iint_{\sigma} \underline{\quad} dS$	Surface integral; integrate with respect to the surface area of σ	
$\int_C \underline{\quad} ds$	Line integral; integrate with respect to arc length of C ; Note that integrals of the form $\oint_C \vec{F} \bullet \vec{T} ds$ can also be expressed as $\oint_C \vec{F} \bullet d\vec{r}$, where $\mathbf{r}(t)$ is the vector equation of C	
$\oint_C \underline{\quad} ds$	Line integral over a closed curve	
$\oint_S \underline{\quad} d\vec{A}$	Physicist's symbol for a surface integral over a closed surface	
$\int_S \underline{\quad} d\vec{A}$	Physicist's symbol for a surface integral over a surface that is not closed.	
$\oint_C \underline{\quad} d\vec{s}$	Physicist's symbol for a line integral over a closed curve.	
$d\vec{A}$	"area vector"	vector-valued function; this is the outward unit normal vector scaled so that its magnitude accounts for the area of the surface; it encompasses the $\vec{n}dS$ from the 3c formulas involving surface integrals
$d\vec{s}$	"arc length vector"	vector-valued function; this is the unit tangent vector scaled so that its magnitude accounts for the arc length; it encompasses the $\vec{T}ds$ or the $d\vec{r}$ from the 3c formulas involving line integrals

Maxwell's Equations

1. Gauss' Law for Electricity	
Integral Form	Differential Form
3c $\underbrace{\Phi_{\mathbf{E}}}_{flux} = \iint_{\sigma} \vec{\mathbf{E}} \cdot \vec{\mathbf{n}} dS = \frac{q_{enc}}{\epsilon_0}$ 4b $\underbrace{\Phi_{\mathbf{E}}}_{flux} = \oint_S \vec{\mathbf{E}} \cdot d\vec{\mathbf{A}} = \frac{q_{enc}}{\epsilon_0}$	$\nabla \cdot \vec{\mathbf{E}} = div(\vec{\mathbf{E}}) = \frac{\rho}{\epsilon_0}$
2. Gauss' law for magnetism	
Integral Form	Differential Form
3c $\Phi_{\mathbf{B}} = \iint_{\sigma} \vec{\mathbf{B}} \cdot \vec{\mathbf{n}} dS = 0$ 4b $\Phi_{\mathbf{B}} = \oint_S \vec{\mathbf{B}} \cdot d\vec{\mathbf{A}} = 0$	$\nabla \cdot \vec{\mathbf{B}} = div(\vec{\mathbf{B}}) = 0$
3. Faraday's Law of Induction	
Integral Form	Differential Form
3c $\oint_C \vec{\mathbf{E}} \cdot \vec{\mathbf{T}} ds = \oint_C \vec{\mathbf{E}} \cdot d\vec{\mathbf{r}} = -\frac{d\Phi_{\mathbf{B}}}{dt}$ 4b $\underbrace{\oint_C \vec{\mathbf{E}} \cdot d\vec{\mathbf{s}}}_{emf} = -\frac{d\Phi_{\mathbf{B}}}{dt} = -\frac{d}{dt} \int_S \vec{\mathbf{B}} \cdot d\vec{\mathbf{A}}$	$\nabla \times \vec{\mathbf{E}} = curl(\vec{\mathbf{E}}) = -\frac{\partial \vec{\mathbf{B}}}{\partial t}$
4. Ampere/Maxwell's Law	
Integral Form	Differential Form
3c $\oint_C \vec{\mathbf{B}} \cdot \vec{\mathbf{T}} ds = \oint_C \vec{\mathbf{B}} \cdot d\vec{\mathbf{r}} = \mu_0 \epsilon_0 \frac{d\Phi_{\mathbf{E}}}{dt} + \mu_0 i_{enc}$ 4b $\oint_C \vec{\mathbf{B}} \cdot d\vec{\mathbf{s}} = \mu_0 \epsilon_0 \frac{d\Phi_{\mathbf{E}}}{dt} + \mu_0 i_{enc}$ $\oint_C \vec{\mathbf{B}} \cdot d\vec{\mathbf{s}} = \mu_0 \epsilon_0 \frac{d}{dt} \int_S \vec{\mathbf{E}} \cdot d\vec{\mathbf{A}} + \mu_0 i_{enc}$	$\nabla \times \vec{\mathbf{B}} = curl(\vec{\mathbf{B}})$ $= \mu_0 i_{enc} + \epsilon_0 \mu_0 \frac{\partial \vec{\mathbf{E}}}{\partial t}$ $= \frac{4\pi k}{c^2} \vec{\mathbf{J}} + \frac{1}{c^2} \frac{\partial \vec{\mathbf{E}}}{\partial t}$ $= \frac{\vec{\mathbf{J}}}{\epsilon_0 c^2} + \frac{1}{c^2} \frac{\partial \vec{\mathbf{E}}}{\partial t}$

Some formulas were taken from the following website:

hyperphysics.phy-astr.gsu.edu/hbase/electric/maxeq.html

Thanks to Kaz Tarui and Katherine Meyer-Canales for their help in developing this handout.