

Test #2

Directions: Please show all your work since partial credit is given. Answers without the necessary work will receive no credit. And remember, have fun!

1. Simplify completely.

+2 a) $\frac{150abc}{45ac}$

$$\boxed{\frac{10b}{3}}$$

$$\frac{150abc \div 15}{45ac \div 15} = \frac{10b}{3}$$

+2 b) $\frac{4}{15}(45x)$

$$= \frac{4}{15} \cdot \frac{45x}{1} = \frac{12x}{1}$$

$$\boxed{12x}$$

+2 c) $\frac{15}{16} \div \frac{25}{32}$

$$\boxed{\frac{6}{5}}$$

$$\frac{15}{16} \cdot \frac{32}{25} = \frac{15 \cdot 32}{16 \cdot 25} = \frac{96}{80}$$

$$= \frac{3 \cdot 32}{16 \cdot 5} = \frac{3 \cdot 2}{5} = \frac{6}{5}$$

+2 d) $\frac{12}{x} - \frac{9}{x} = \frac{3}{x}$

$$\boxed{\frac{3}{x}}$$

+2 e) $-6 + \frac{3}{4}$

$$\boxed{-\frac{21}{4} \text{ or } -5\frac{1}{4}}$$

+2 f) $\frac{7}{15} + \frac{2}{3} + \frac{4}{5}$

$$\boxed{\frac{29}{15}}$$

$$\frac{7}{15} + \frac{10}{15} + \frac{12}{15}$$

$$\frac{17+12}{15} = \frac{29}{15}$$

$$-\frac{24}{4} + \frac{3}{4} = -\frac{21}{4}$$

+12

2. Convert the following to improper fractions.

+2 a) $4\frac{3}{5}$
 $= \frac{4 \cdot 5 + 3}{5}$

$$\boxed{\frac{23}{5}}$$

+2 b) $-12\frac{3}{4}$
 $= -\frac{4 \cdot 12 + 3}{4}$

$$\boxed{-\frac{51}{4}}$$

3. A board that was $95\frac{3}{8}$ inches long had a piece, $3\frac{15}{16}$ inches long, cut off from one end. What is the length of the board now?

+2

$$95\frac{3}{8} - 3\frac{15}{16} = \frac{763}{8} - \frac{63}{16}$$

$$= \frac{1526}{16} - \frac{63}{16}$$

$$\boxed{= \frac{1463}{16} = 91\frac{7}{16} \text{ inches}}$$

+2 4. A recipe calls for $1\frac{3}{4}$ cups of sugar. How much sugar is needed if the recipe is tripled?

$$\boxed{5\frac{1}{4} \text{ cups}}$$

$$\left(1\frac{3}{4}\right) \cdot 3$$

$$\frac{7}{4} \cdot \frac{3}{1} = \frac{21}{4}$$

$$= 5\frac{1}{4}$$

+8

5. Simplify the following expressions. Make sure to reduce all fractions to lowest terms.

+2 a) $6 \div 2\frac{1}{4}$ _____

$$6 \div \left(\frac{9}{4}\right) = \frac{6}{1} \cdot \frac{4}{9}$$

$$= \frac{8}{3} \text{ or } 2\frac{2}{3}$$

+2 c) $4\frac{2}{9} - 1\frac{7}{18}$ _____

$$\frac{38}{9} - \frac{25}{18}$$

$$\frac{76}{18} - \frac{25}{18}$$

$$\frac{51}{18} \div 3$$

$$\frac{17}{6}$$

$$\frac{17}{6}$$

+2 b) $5 + 3\left(5\frac{1}{2}\right)$ _____

$$5 + 3 \cdot \frac{11}{2}$$

$$= 5 + \frac{33}{2}$$

$$= \frac{10}{2} + \frac{33}{2}$$

$$= \frac{43}{2} \text{ or } 21\frac{1}{2}$$

+2 d) $\left(\frac{1}{10} + 2\frac{3}{5}\right)\left(3\frac{1}{2} - 1\frac{2}{3}\right)$ _____

$$\left(\frac{1}{10} + \frac{26}{10}\right) \cdot \left(\frac{21}{6} - \frac{10}{6}\right)$$

$$\frac{27}{10} \cdot \frac{11}{6} = \frac{297}{60}$$

$$\frac{99}{20} \text{ or } 4\frac{19}{20}$$

$$\text{or } \frac{297}{60}$$

+8

- +2 6. A basketball team missed about $\frac{3}{5}$ of their 85 free throws in a game. How many free throws did they *make*? 17

$$\underline{\text{Misses}} \quad \frac{85}{1} \cdot \frac{3}{5} = \frac{85 \cdot 3}{1 \cdot 5} = 17 \cdot 3 = 51$$

$$\text{Made} = 85 - 51 = 34$$

34 makes

- +2 7. A rope $12\frac{2}{3}$ feet long is divided into 5 pieces. How long is each piece?

$$\left(12\frac{2}{3}\right) \div 5 = \frac{38}{3} \cdot \frac{1}{5} = \frac{38}{15}$$

$$\frac{38}{15} \text{ or } 2\frac{8}{15} \text{ feet}$$

8. Evaluate each expression for the given value.

+2 a) $4y - 12$ if $y = -5$ _____

$$4 \cdot (-5) - 12$$

$$-20 - 12$$

$$-32$$

+2 b) $-x + 3$ if $x = -2$ _____

$$-(-2) + 3$$

$$2 + 3$$

$$5$$

+8

9. Simplify completely.

a) $7x - 3x + 7 - 9$ _____

$$\boxed{4x - 2} + 2$$

b) $4(2y - 2) + 5(y + 2)$ _____

$$8y - 8 + 5y + 10 + 2$$

$$\boxed{13y + 2}$$

c) $0.46 + 1.058 + 5$

$$\boxed{6.518}$$

$$\begin{array}{r} 5.000 \\ 0.460 \\ + 1.058 \\ \hline 6.518 \end{array} + 2$$

d) $9.758 - 12.022$

$$\boxed{-2.264}$$

$$\begin{array}{r} 12.022 \\ - 9.758 \\ \hline 2.264 \end{array} + 2$$

+8

e) $(-5.05)(-0.074)$ +0.3737

$$\begin{array}{r} \overset{3}{5.05} \\ \times 0.074 \\ \hline 2020 \\ 35350 \\ \hline 37370 \end{array} \quad +2$$

f) $8.184 \div (-3.1)$ = -2.64

$$\begin{array}{r} 8.184 \\ -3.1 \\ \hline 81.84 \\ 31 \\ \hline 2.64 \\ 31 \overline{) 81.84} \\ \underline{-62} \\ 198 \\ \underline{186} \\ 124 \\ \underline{-124} \\ 0 \end{array} \quad +2$$

g) $4.2 - 4(0.16)$ _____

$$4.2 - 0.64 \quad +2$$

3.56

h) $45.45 + 3(2.1 - 3.75)$ 40.5

$$45.45 + 3 \cdot (-1.65) \quad +2$$

$$45.45 - 4.95$$

$$40.5$$

+8

10. Is $t = 3$ a solution to $2t - 5 = 11$? Why or why not?

No

$$+2 \quad 2 \cdot 3 - 5 = 6 - 5 = 1 \neq 11$$

11. Solve the following equations.

a) $2a - 6a + a = 15$ _____

$$-4a + 1a = 15$$

$$-3a = 15$$

+2

$$\frac{-3a}{-3} = \frac{15}{-3}$$

$$a = -5$$

b) $3(b - 7) - 2b = -24$ _____

$$3b - 21 - 2b = -24$$

$$b - 21 = -24$$

$$+2 \quad +21 \quad +21$$

$$b = -3$$

c) $4(3b - 4) + 14 = 22$ _____

$$12b - 16 + 14 = 22$$

$$+2 \quad 12b - 2 = 22$$
$$+2 \quad +2$$

$$\frac{12b}{12} = \frac{24}{12}$$

$$b = 2$$

d) $-6x + 4 = 26$ _____

$$-4 \quad -4$$

$$-6x = 22$$

$$+2 \quad \frac{-6x}{-6} = \frac{22}{-6}$$

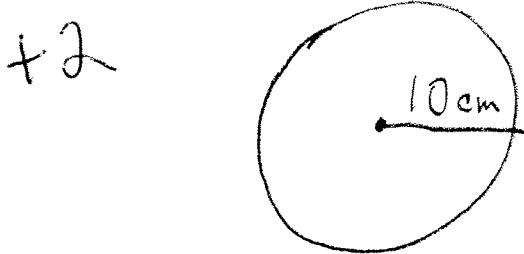
$$x = \frac{-22}{6} \div 2$$
$$6 \div 2$$

$$x = \frac{-11}{3} \text{ or } -3\frac{2}{3}$$

+10

12. The following questions are about a circle with radius 10 centimeters (cm). Use the approximation $\pi \approx 3.14$ in your calculations.

a) Draw the circle, and clearly label the radius.



b) Find the circumference of the circle. Make sure to include the appropriate units.

+2

$$C = \boxed{62.8 \text{ cm}}$$

$$\begin{aligned} C &= \pi \cdot D \\ &= (3.14) \cdot 20 \\ &= 62.8 \end{aligned}$$

$$\begin{aligned} \text{Diameter} &= 2 \cdot (\text{radius}) \\ D &= 2 \cdot 10 = 20 \end{aligned}$$

$$\begin{array}{r} 3.14 \\ \times 20 \\ \hline 62.80 \end{array}$$

c) Find the area of the circle.

+2

$$A = \boxed{314 \text{ cm}^2}$$

$$\begin{aligned} A &= \pi \cdot r^2 \\ &= 3.14 \cdot (10)^2 \\ &= 3.14 \cdot (100) \\ &= 314 \end{aligned}$$

+6