

Percent Problems

Objective 1 Solve a Basic Percent Problem

Basic percent problems are problems that are generally given as a simple word statement.

For example, suppose you were asked the question, "what number is 50% of 20?"

To solve this basic percent problem, we want to translate the given word statement into a mathematical equation using a variable to represent the unknown quantity. Then we solve the equation and answer the question.

Let's now translate the question "what number is 50% of 20?" into an equation.

$$\begin{array}{ccccccccc}
 \text{What} & \text{number} & \text{is} & 50\% & \text{of} & 20? \\
 \swarrow & & \swarrow & \downarrow & \downarrow & \downarrow \\
 x & = & 0.50 & \cdot & 20
 \end{array}$$

Notice that the unknown number is represented by x , the "is" by an equals sign, 50% by 0.50, "of" by a multiplication symbol, and the 20 represents itself.

The equation $x = 0.50 \cdot 20$ tells us that $x = 10$. So to properly answer the question, what number is 50% of 20, we should write:

10 is 50% of 20.

Example 1: What is 38% of 90?

Suppose we are asked to the question, what percent of 48 is 12? Again, we want to translate the given word statement into a mathematical equation using a variable to represent the unknown quantity.

What percent of 48 is 12?
 $x \cdot 48 = 12$

Here we have the equation $x \cdot 48 = 12$ or $48x = 12$. Solving for x we get, $x = \frac{1}{4}$ or $x = 0.25$.

Because x in this problem represents a percent, we convert the decimal number to a percent by moving the decimal point two places to the right. This gives us $x = 25\%$.

To properly answer the question, we write the following: **25% of 48 is 12.**

Example 2: What percent of 32 is 20?

Example 3: 29 is 4% of what number?

$$29 = 0.04 \cdot x$$

Example 4: 30% of 60 is what number?

$$0.30 \cdot 60 = x$$

Example 5: What percent of 91 is 52? Round your final answer to the nearest tenth of a percent.