

# Rationalizing the Denominator: Part 1

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In mathematics, it is sometimes easier to work with radical expressions if the denominator does not have any radicals.

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Example 1:

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$$\frac{1}{\sqrt{2}}$$

Multiplying  $\frac{1}{\sqrt{2}}$  by  $\frac{\sqrt{2}}{\sqrt{2}}$  will eliminate the radical in the denominator:

$$\frac{1}{\sqrt{2}} \left( \frac{\sqrt{2}}{\sqrt{2}} \right) = \boxed{\frac{\sqrt{2}}{2}}$$

This process of eliminating the radical in the denominator is called **Rationalizing the Denominator**.

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Example 2:

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Rationalize the Denominator

a.)  $\frac{4}{\sqrt{3}}$

b.)  $\frac{\sqrt{2}}{\sqrt{6}}$

c.)  $\frac{8}{\sqrt{x}}$

d.)  $\sqrt{\frac{1}{3}}$

## Rationalizing the Denominator with Cube Roots

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Example 3:

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Rationalize the Denominator:

a.)  $\frac{2}{\sqrt[3]{5}}$

Here, multiplying the top and the bottom by  $\sqrt[3]{5^2}$  will rationalize the denominator since:  $\sqrt[3]{5} \cdot \sqrt[3]{5^2} = \sqrt[3]{5^3} = 5$

$$\frac{2}{\sqrt[3]{5}} \left( \frac{\sqrt[3]{5^2}}{\sqrt[3]{5^2}} \right) = \frac{2\sqrt[3]{5^2}}{5} = \boxed{\frac{2\sqrt[3]{25}}{5}}$$

b.)  $\frac{\sqrt[3]{3}}{\sqrt[3]{4}}$

# Rationalizing the Denominator Part 1

## Practice Problems

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Rationalize each Denominator:

1.  $\sqrt{\frac{1}{5}}$

2.  $\frac{9}{\sqrt{x}}$

3.  $\frac{\sqrt[3]{5}}{\sqrt[3]{2}}$

4.  $\frac{\sqrt[3]{4}}{\sqrt[3]{x^2}}$